1.

$$C(x,t) = C_0 \left(1 - erf \frac{x}{2\sqrt{D_{ap}t}} \right) + C_{initial}$$

上記の塩化物イオン濃度の予測式を C_0 について解くと、By solving the above equation for predicting chloride ion concentration for C_0 ,

$$C_0 = \frac{C(x,t) - C_{initial}}{1 - erf \frac{x}{2\sqrt{D_{ap}t}}}$$

使用する単位をm, kg, yearsとして以下の値を上式に代入して, By unifying the used units as m, kg and years and substituting the values below to the above equation,

$$x = 0.03m$$
, $C(0.03m, 10 years) = 1.0 kg/m^3$, $C_{initial} = 0$, $D_{ap} = 0.5 \times 10^{-4} m^2/year$, $t = 10 years$ $C_0 \approx 2.92 kg/m^3$

2.

鉄筋位置の塩化物イオン濃度が腐食発生限界濃度に達するとき、以下の関係が成り立つ. When chloride ion concentration at the location of rebar reaches to the critical chloride ion concentration, the following equation is satisfied.

$$x = 0.05m$$
, $C = C_{lim} = 1.2 \, kg/m^3$, $C_{initial} = 0$, $D_{ap} = 0.5 \times 10^{-4} \, m^2/year$, $C_0 = 2.92 \, kg/m^3$
 $1.2 = 2.92 \times \left(1 - erf \frac{0.05}{2\sqrt{0.5} \times 10^{-4} \times t}\right)$
 $\therefore erf\left(\frac{3.54}{\sqrt{t}}\right) = 0.59 = \beta$

tの値を次々に仮定して、収束計算を行う。ここでは、二分法を用いる。Iteration process is conducted by assuming the value of t again and again. Here, the bi-section method is used.

二分法で用いるtの初期値を $t_1 = 1$ years, $t_2 = 50$ yearsとし,以下の収束条件を用いる. Iteration process is conducted by assuming the value of t again and again. Here, the bi-section method is used.

$$\frac{\left|\beta - erf\left(\frac{3.54}{\sqrt{t}}\right)\right|}{\beta} \times 100 < 0.1$$

(βの誤差が0.1%以下 Error of the value of β is less than 0.1%)

繰返し数9回目で上記の収束条件を満たし, $t = 36.9 \ years$ を得る. The above condition is satisfied at the 9th iteration and $t = 36.9 \ years$ is obtained.

10年目の現在から「あと何年で C_{lim} に達するか」という問いなので、余寿命は 36.9-10=26.9年である. Since the question is how many years it takes until it reaches to C_{lim} from the present, which 10 years have already passed, the remaining life is 36.9-10=26.9 years.

なお、現時点(建設後10年目)と、さらに26.9年経過後の塩化物イオン濃度の分布は、以下のようになる. The chloride ion distribution at present (10 years after the construction) and that after 26.9 years more become as the graph below.

