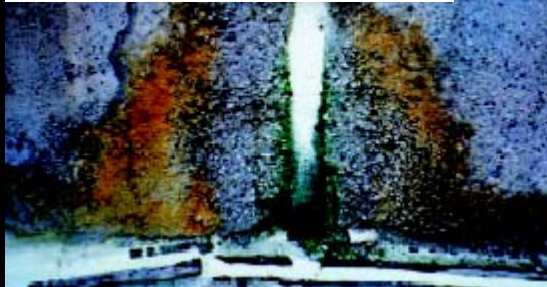


# Modeling of Deformation Behavior of Concrete under Fatigue Loading

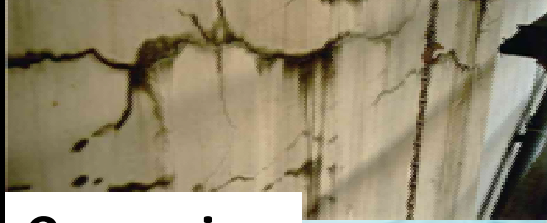
Yasuhiko SATO and Koji MATSUMOTO  
(Hokkaido University)

# Deterioration Mechanism and Performance of Structures

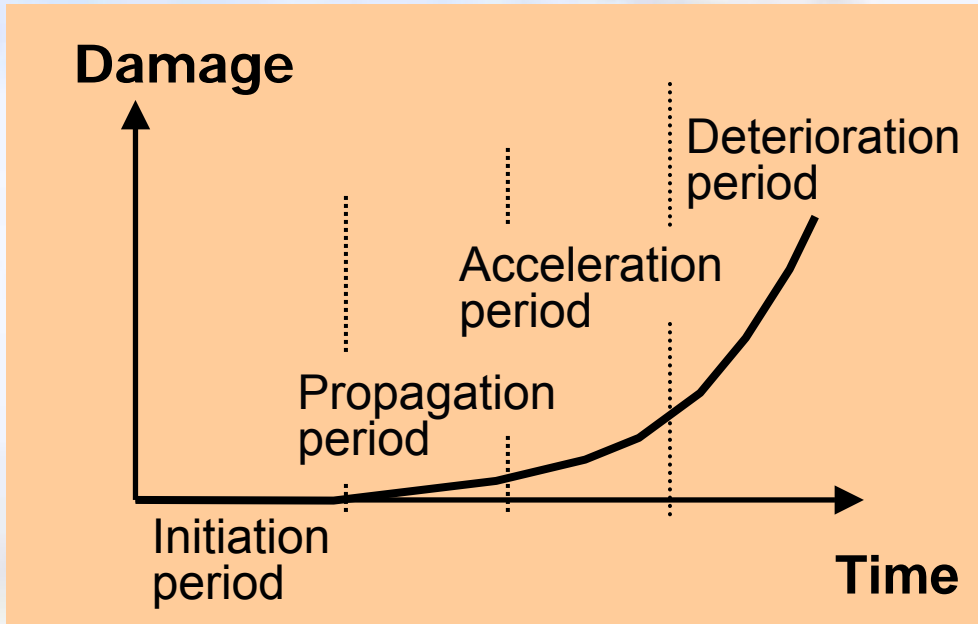
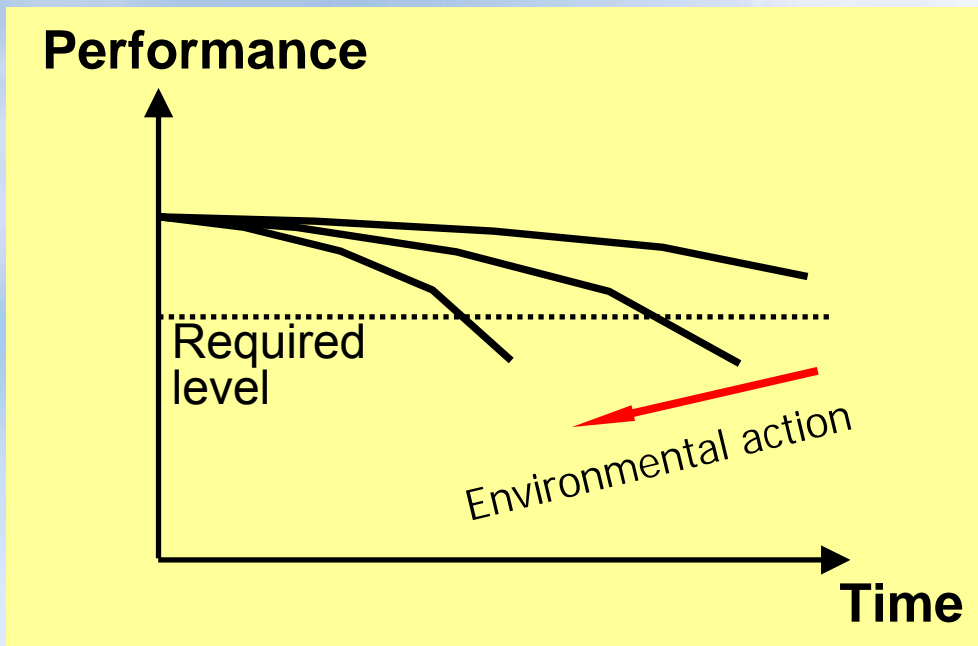
**Chemical attack**



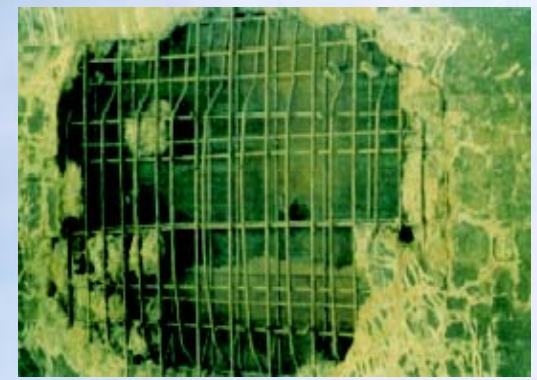
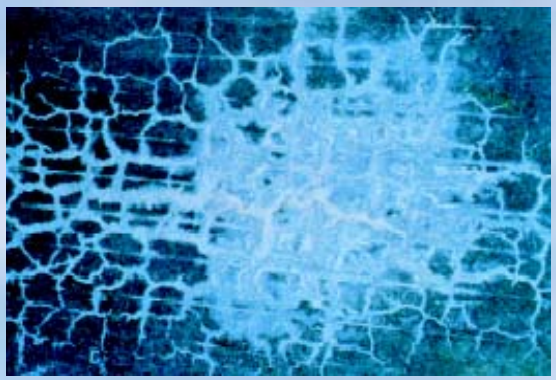
**Alkali-aggregate reaction**



**Corrosion**



# Fatigue - one of the major deterioration mechanism

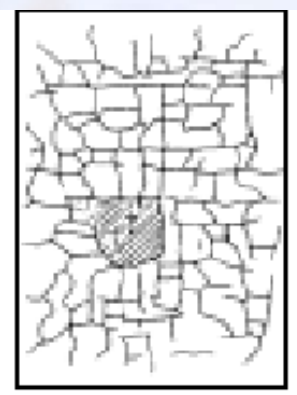
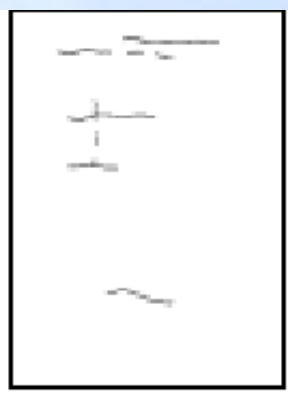


**Initiation period**

**Propagation period**

**Acceleration period**

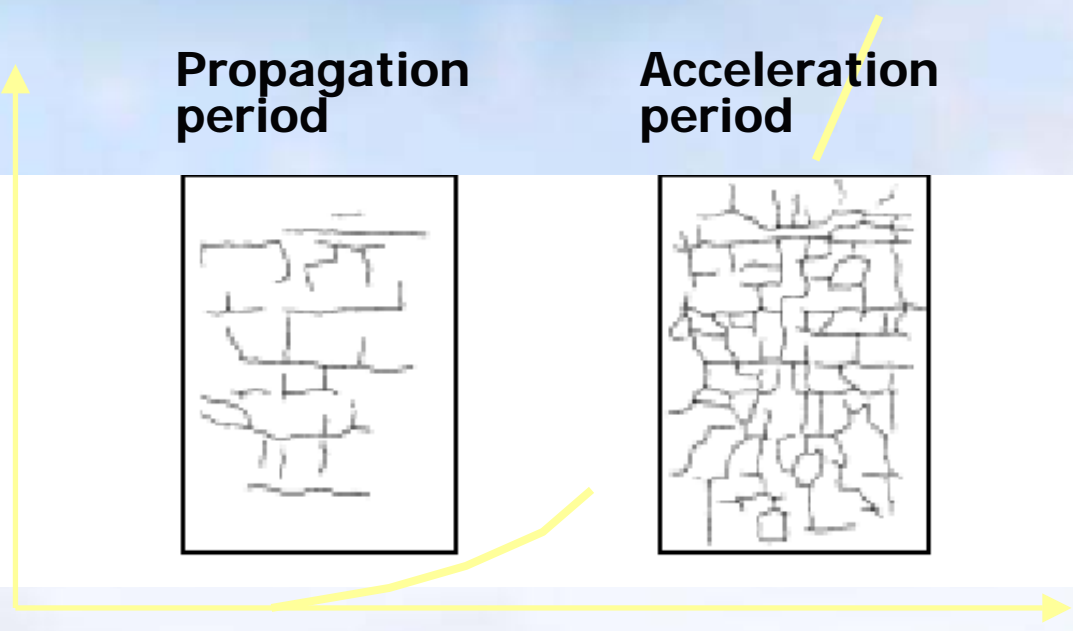
**Deterioration period**



**Flexural cracking**

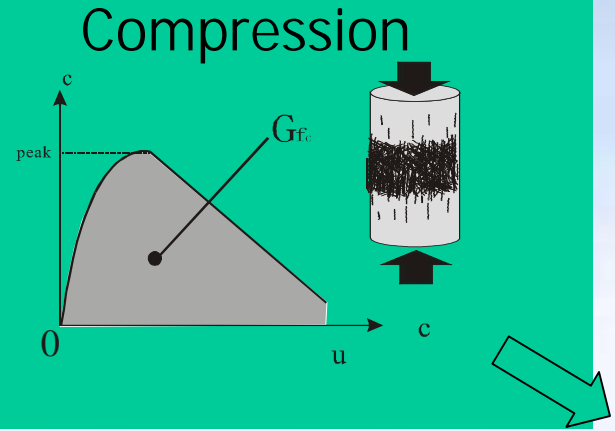
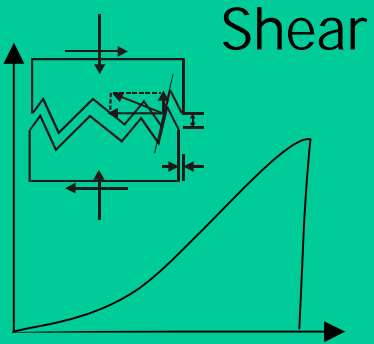
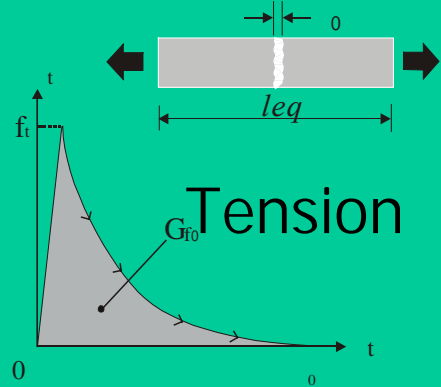
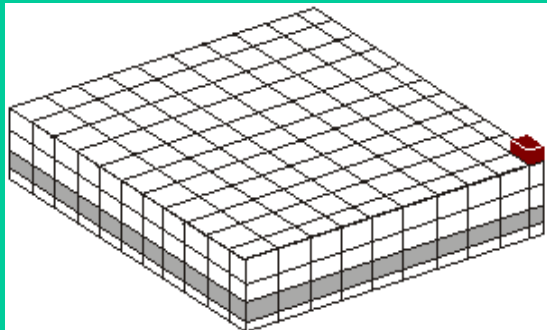
**Hexagonal cracking pattern**

**Punching failure**

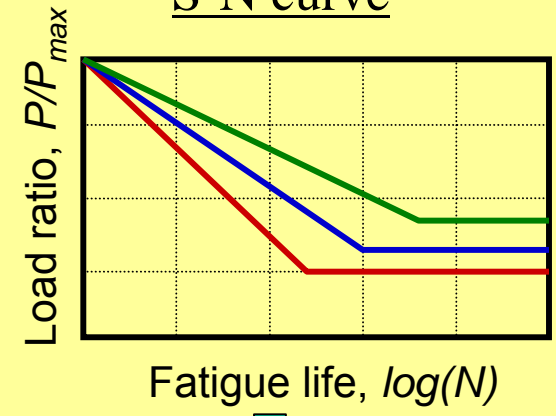


# Necessity of Advanced Prediction Method

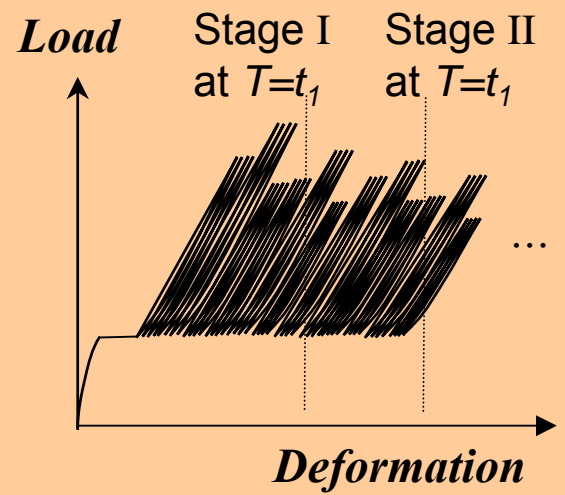
## Shear Capacity Verification using FE Analysis



## S-N curve



## Damage Procedure Fatigue life prediction



# Outline of Study

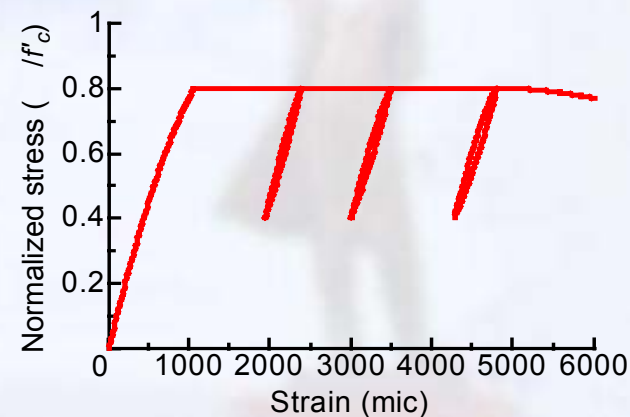
**Experiments for understanding stiffness degradation and strain development under compressive sustained and cyclic loading**



Elasto-plastic and fracture (EPF) model proposed by prof. Maekawa

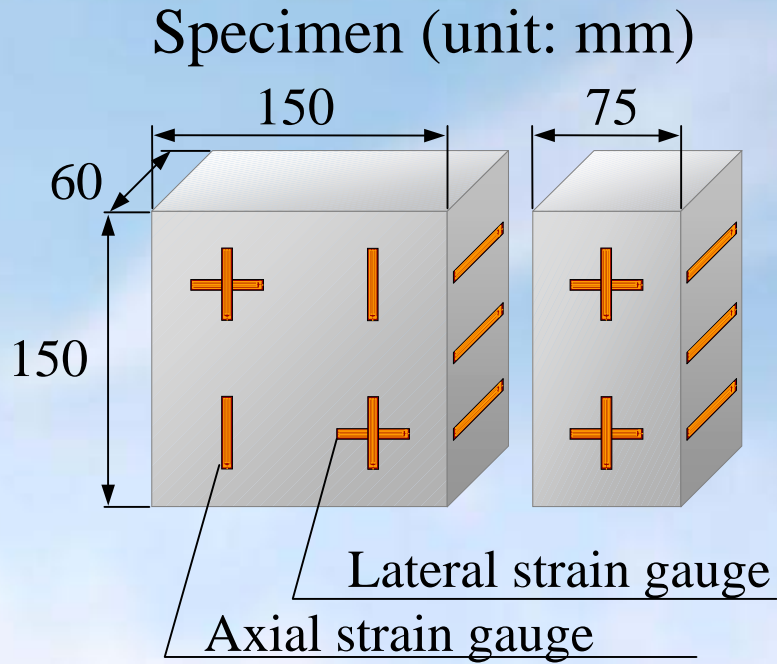
## **Modeling of fatigue behavior**

- Sustained and fatigue
- Stress-strain curve and fatigue life
- Humidity and temperature





# Outline of Experiment



No.	Max stress ratio (%)	Min stress ratio (%)
S1	57	57
S2	62	62
S3	71	71
S4	80	80
S5	90	90
S6	90	90
S7	60	20
S8	60	40
S9	70	15
S10	70	30

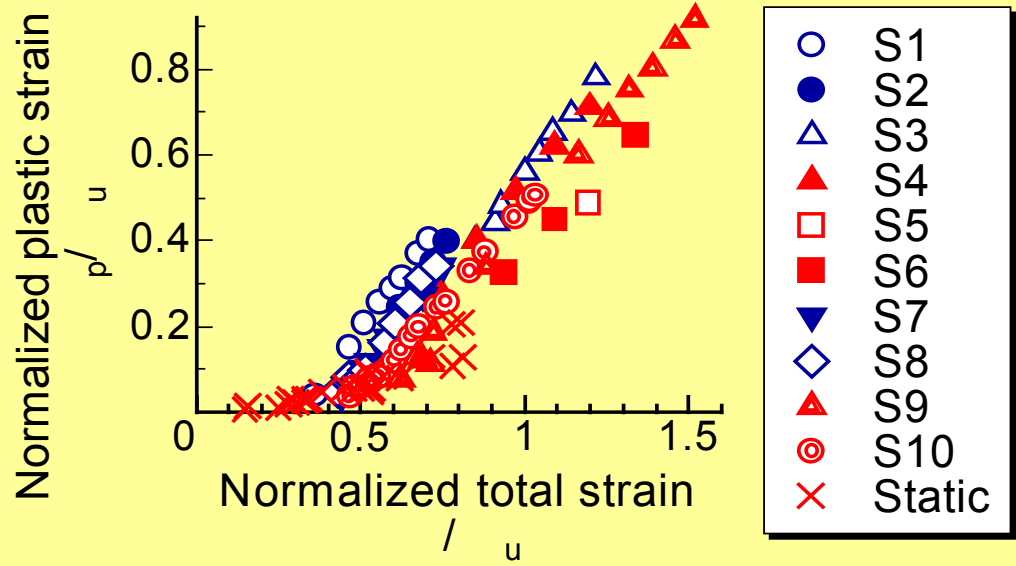
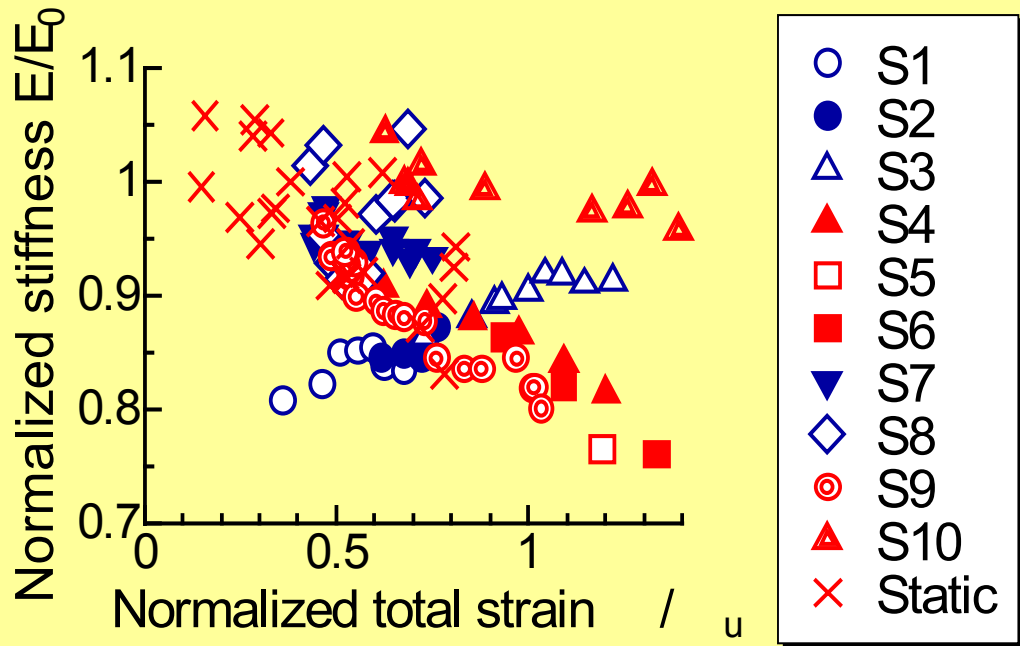
Sustained loading

Cyclic loading

Mix proportion

W/C=60, s/a=41%  
 C=266.7 (kg/m<sup>3</sup>)  
 W=160.0 (kg/m<sup>3</sup>)

# Experimental Results and Discussion (1)



## Stiffness reduction

High stress :  
 → decrease

Low stress :  
 → contact

## Plastic strain

Lower stress :  
 → Higher increment

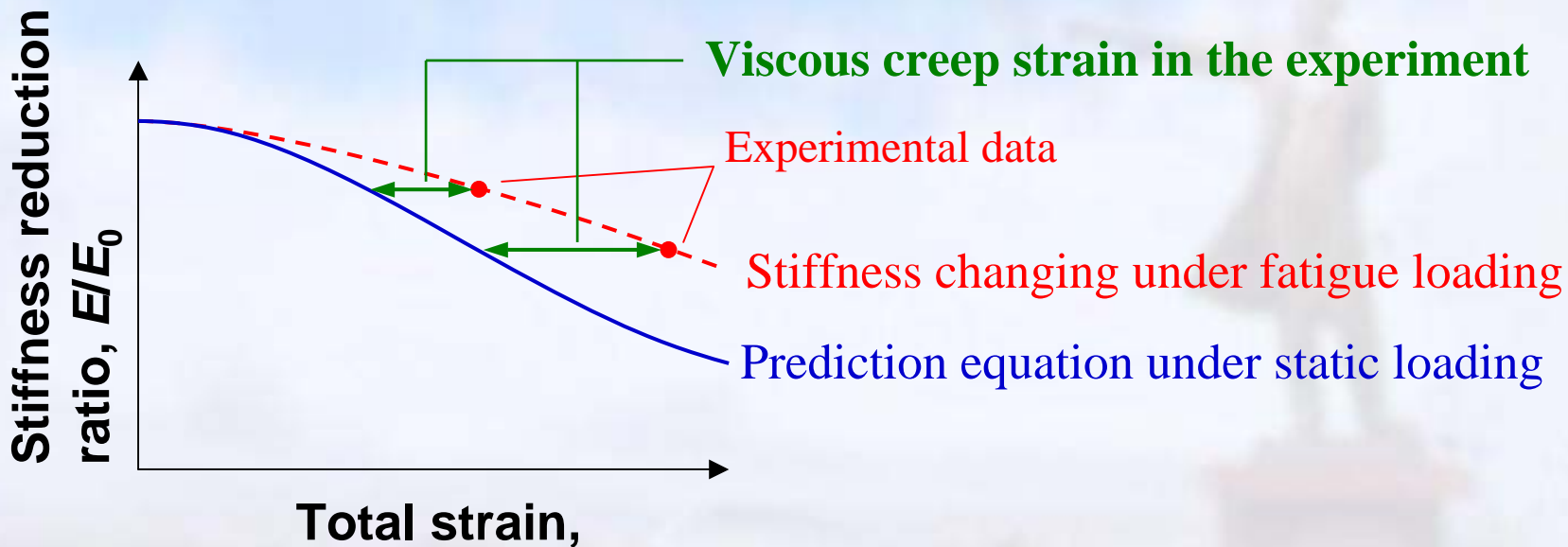
# Experimental Results and Discussion (2)

## Viscous creep strain

Total strain = Cracking strain (Crack propagation) + Viscous creep strain (Consolidation of mortar)

It reduces concrete stiffness

It does not affect concrete stiffness

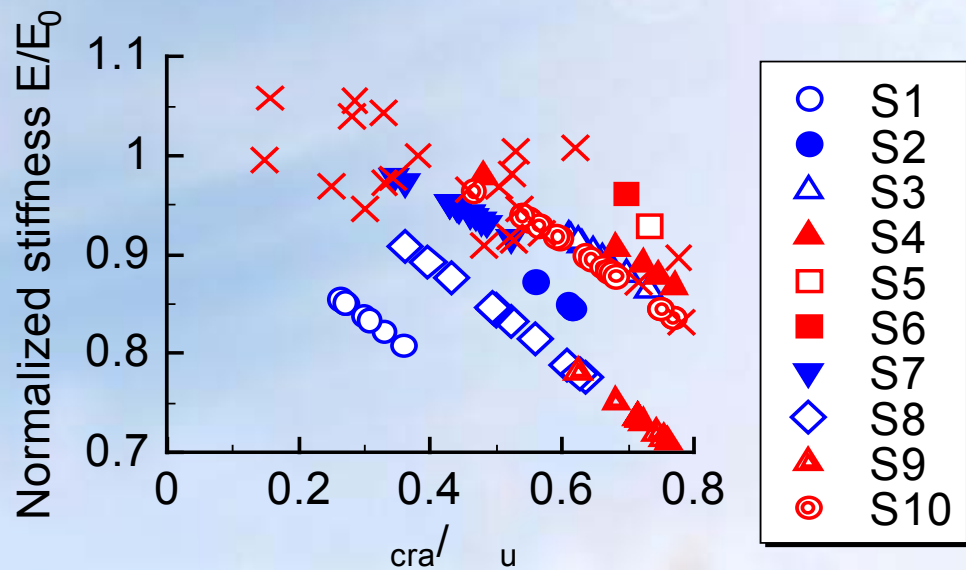




# Experimental Results and Discussion (3)

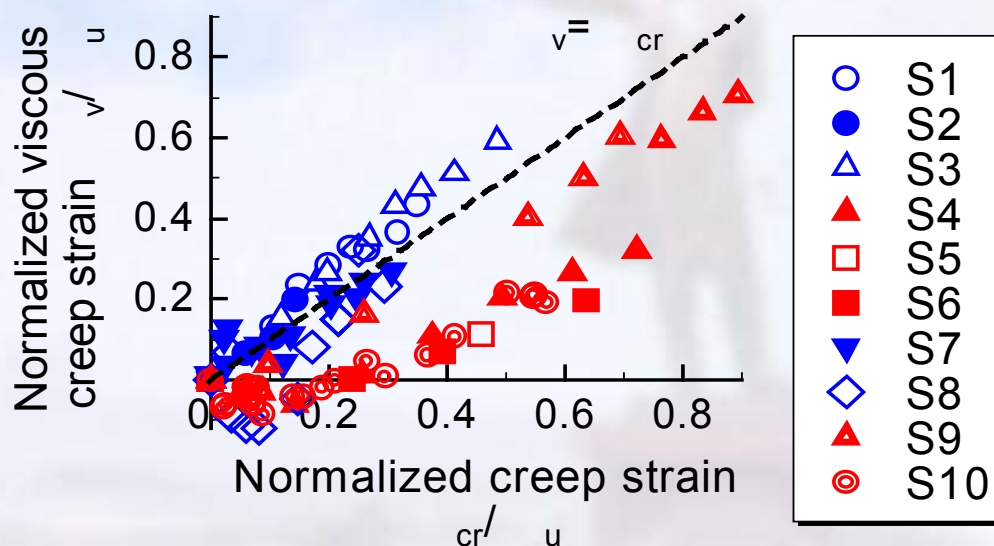
## 3. Stiffness and cracking strain

✓ Stiffness reduction can be expressed as cracking strain, which is deducted viscous creep strain from total strain.



## 4. Viscous creep strain

✓ Lower stress condition, ratio of viscous creep strain is higher.



# MODELING(1)

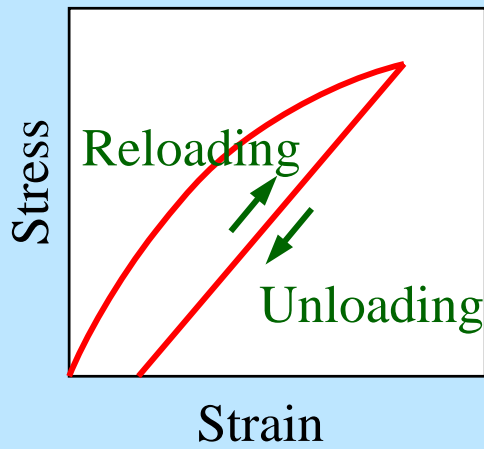
## Elasto-plastic fracture (EPF) model

$$\frac{\sigma}{f'_c} = E_0 K_0 \frac{\varepsilon_e}{\varepsilon'_u} = E_0 K_0 \frac{\varepsilon - \varepsilon_p}{\varepsilon'_u}$$

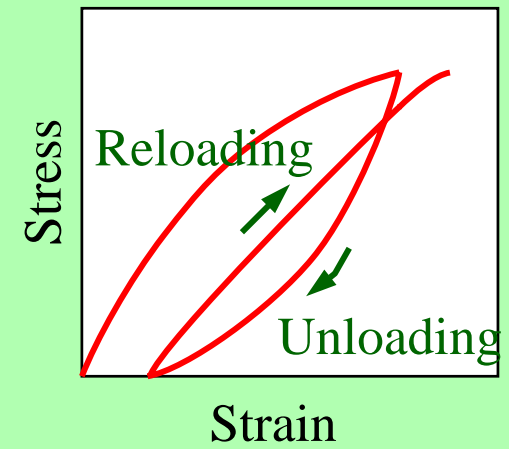
Fracture parameter  $K_0 = \exp\left[-0.73 \frac{\varepsilon_t}{\varepsilon'_u} \left\{1 - \exp\left(-1.25 \frac{\varepsilon_t}{\varepsilon'_u}\right)\right\}\right]$

Plastic strain  $\varepsilon_p = \frac{\varepsilon_t}{\varepsilon'_u} - \frac{20}{7} \left[1 - \exp\left(-0.35 \frac{\varepsilon_t}{\varepsilon'_u}\right)\right]$

## Fatigue model



**Time Effect**

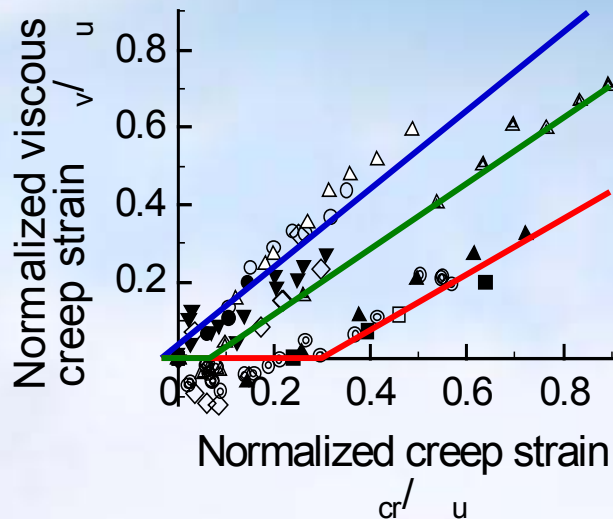


# MODELING(2)

## 1. Fracture parameter under fatigue loading

It be expressed as cracking strain,  $\epsilon_{cra} = \epsilon - \epsilon_v$  ( $\epsilon_v$ : viscous creep strain)

### Viscous creep strain equation (bi-liner model)



When  $S_{max} < 0.12R + 0.6$

$$\epsilon_v = \epsilon_{cr}$$

When  $S_{max} > 0.12R + 0.6$

When  $\epsilon_{cr} < l$

$$\epsilon_v = 0$$

When  $\epsilon_{cr} > l$

$$\epsilon_v = a(\epsilon_{cr} - l)$$

Where,  $l = 20(25S_{max} - 3R - 15)/187$

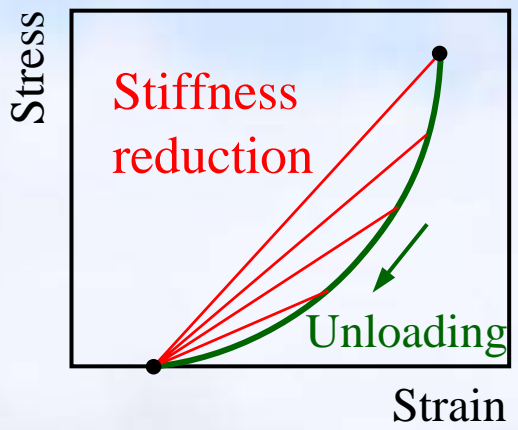
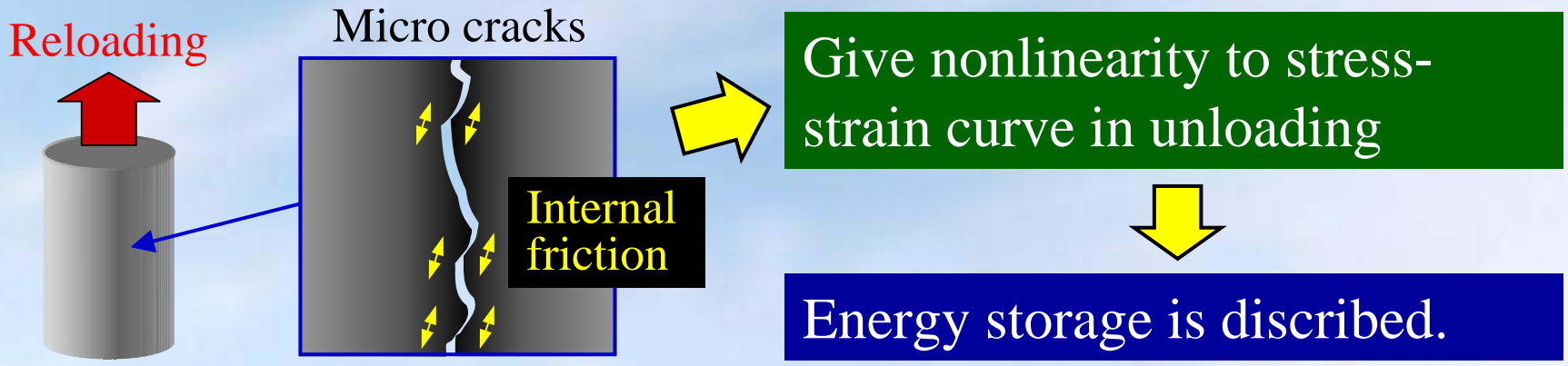
$$a = (-625S_{max} + 75R + 562)/187$$

However,  
 $l < 0 \Rightarrow l = 0$   
 $a < 0 \Rightarrow a = 0$   
 $a > 1 \Rightarrow a = 1$

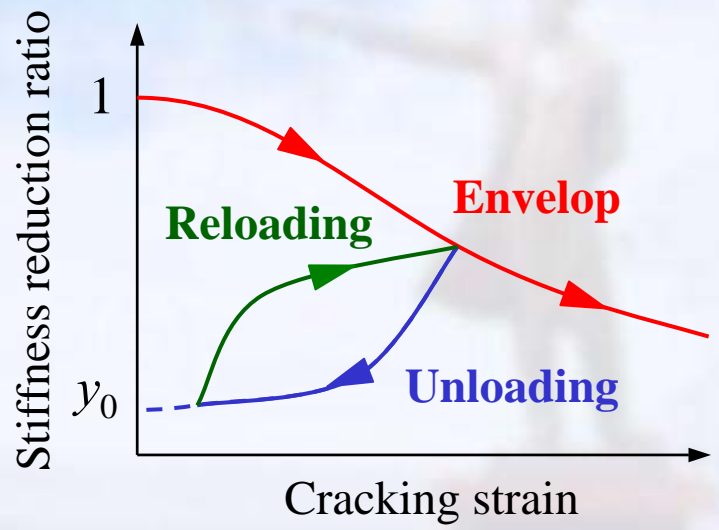
$$\text{Fracture parameter } K_0 = \exp \left[ -0.73 \frac{\epsilon_t - \epsilon_v}{\epsilon'_u} \left\{ 1 - \exp \left( -1.25 \frac{\epsilon_t - \epsilon_v}{\epsilon'_u} \right) \right\} \right]$$

# MODELING(3)

## 2. Stiffness changing in unloading and reloading



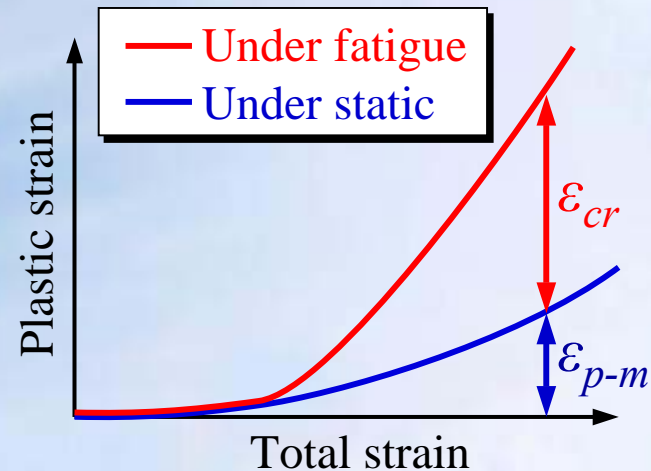
Stiffness decreases visually



### 3. Plastic strain under fatigue loading

Plastic strain under fatigue loading  
 = Time-independent plastic strain  
 + Time-dependent plastic strain

$$\varepsilon_p = \varepsilon_{p-m} \text{ (Maekawa's equation)} + \varepsilon_{cr} \text{ (Creep strain prediction equation)}$$



#### Modified Ayano's equation (creep strain prediction equation)

$$\varepsilon_{cr} = c_y \cdot c_e \cdot \varepsilon(t, t', t_0)$$

$c_y$ : Coefficient for effect of cyclic loading

$$c_y = \frac{1+R}{2} (1 + 3.87\Delta)$$

$c_e$ : Coefficient for effect of environmental condition

$$c_e = \frac{4W(1-h) + 350}{587} (0.0133T + 0.733) \quad \varepsilon(t, t', t_0): \text{Ayano's creep strain prediction equation}$$

$$R = \frac{\sigma_{\min}}{\sigma_{\max}}, \quad \Delta = \frac{\sigma_{\max} - \sigma_{\min}}{f'_c}$$

Considered with temperature and humidity  
 Applicable to fatigue loading



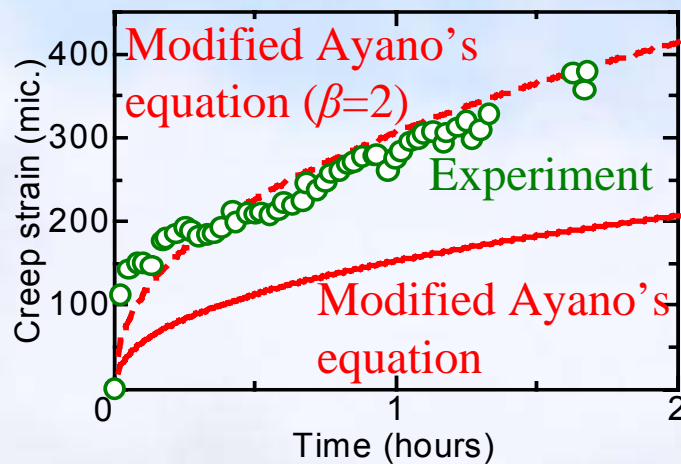
# MODELING(5)

## Creep strain under high stress

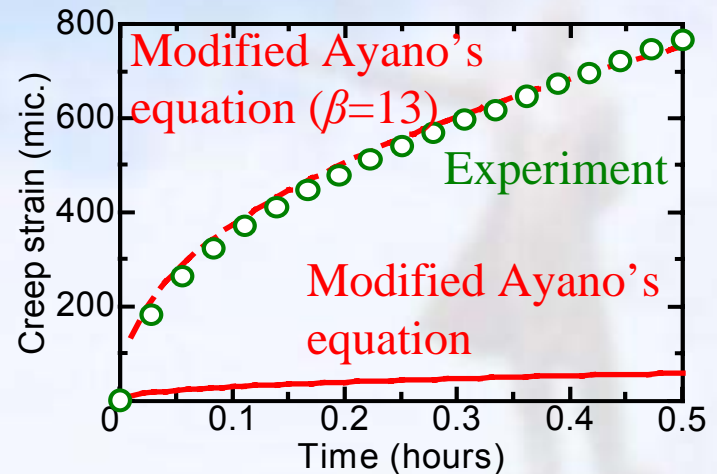
Applicable range of modified Ayano's equation: stress ratio ~50%

It cannot be applied for high stress

**Creep strain caused by cracking should be quantified.  
But it is expressed as multiplying coefficient  $\beta$  which is  
determined by experimental data.**



S9 ( $S_{\max}=65\%$ ,  $S_{\min}=0\%$ )



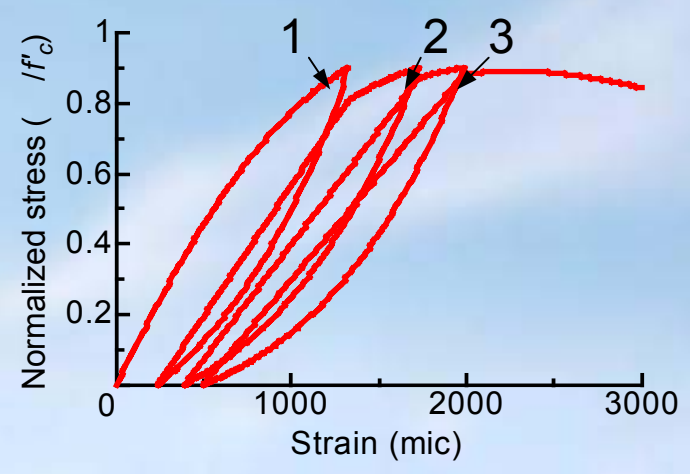
S5 ( $S=90\%$ )

# Parametric Study(1)

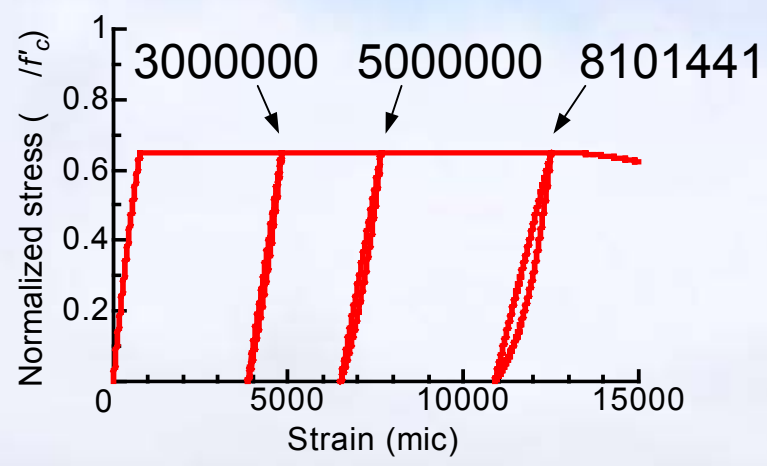
No.	Max stress ratio (%)	Max stress ratio (%)	Temperature (deg)	Relative humidity (%)	Multiplying coefficient $\beta$ for creep strain prediction equation
S1	80	0	20	70	20
S2			35	15	
S3			5	100	
S4	80	20	20	70	15
S5		40			10
S6		60			5
S7	90	0	20	70	30
S8	65				2

# Computed Results(1)

## Influence of Maximum Stress

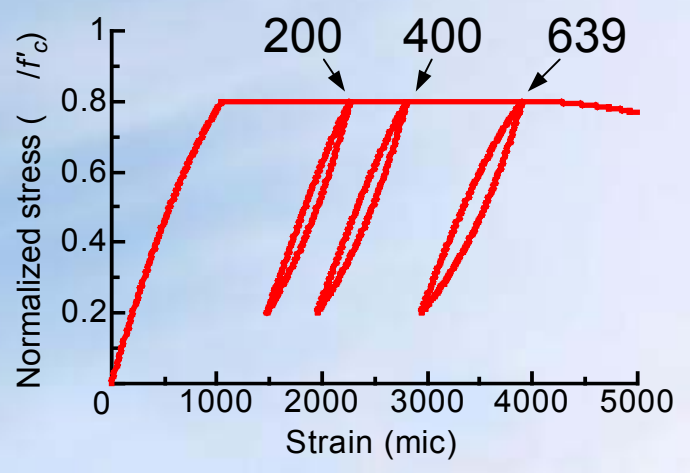


S7 (90%-0%, T=20 , h=70%)

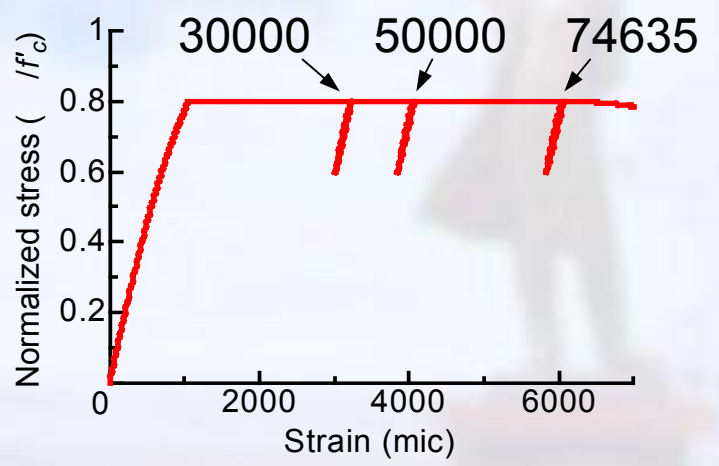


S9 (65%-0%, T=20 , h=70%)

## Influence of Minimum Stress



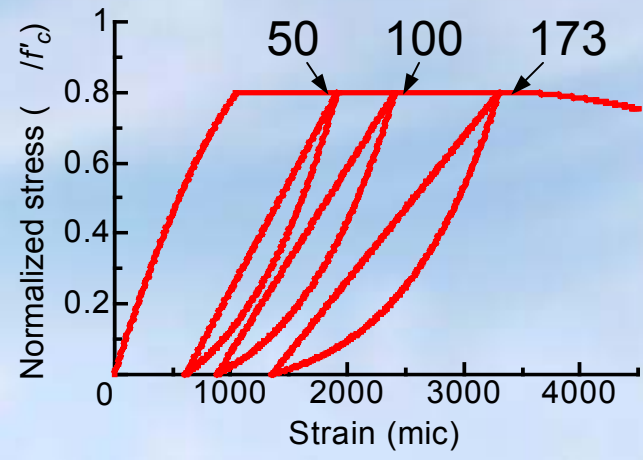
S4 (80%-20%, T=20deg, h=70%)



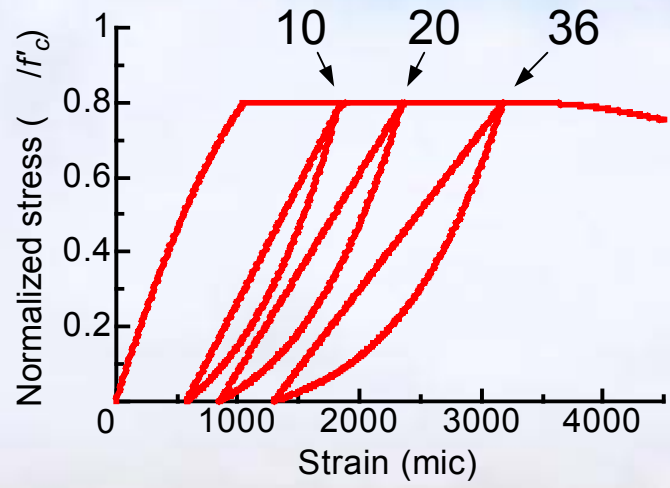
S6 (80%-60%, T=20deg, h=70%)

# Computed Results (2)

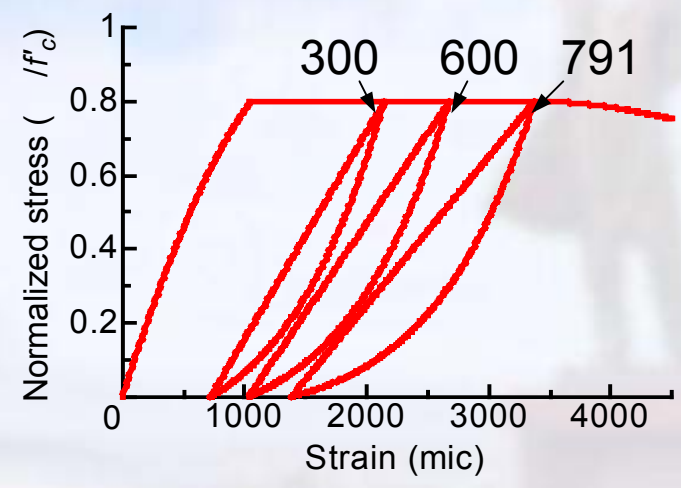
## Effect of environmental condition



S1 (80%-0%, T=20deg, h=70%)



S2 (80%-0%, T=35deg, h=15%)

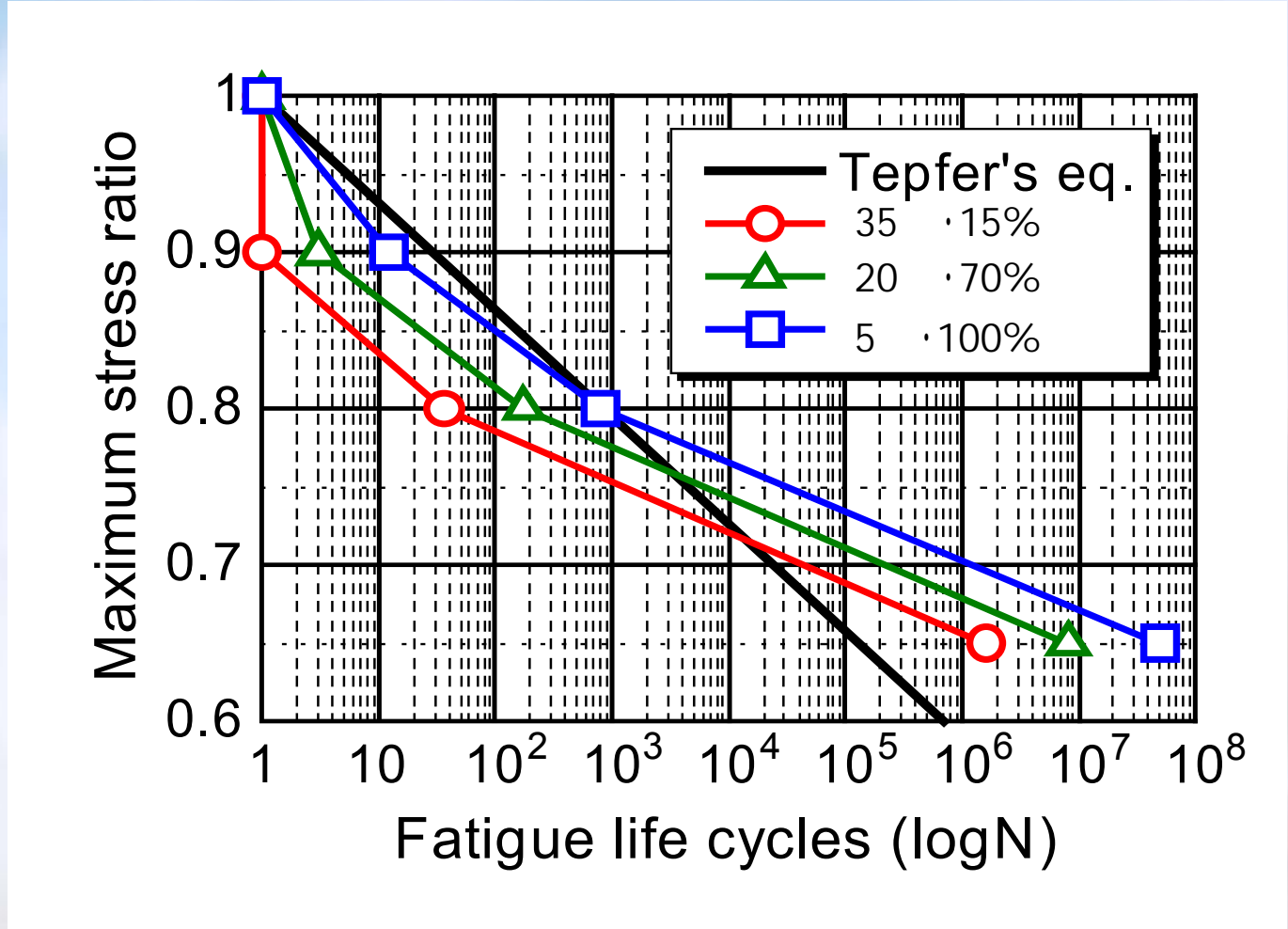


S3 (80%-0%, T=5deg, h=100%)

# Fatigue Life

Tepfers's equation

$$\frac{\sigma_{\max}}{f'_c} = 1 - 0.0685 \left( 1 - \frac{\sigma_{\min}}{\sigma_{\max}} \right) \log_{10} N$$





***Stress – strain curves of concrete under compressive sustained and fatigue loading***

- /Strain components : Cracking strain  
  Viscous creep strain**
- /Stiffness reduction : Cracking strain**

***Parametric Study using the Model***

- /Fatigue life influenced by humidity and temperature**